Wrapper Induction for Information Extraction

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Abstract
Many Internet information resources present relational data—telephone directories, product catalogs, etc. Because these sites are formatted for human browsing (e.g., an HTML page), rather than for use by a program. Therefore, software systems using such resources (e.g., heterogeneous database systems [Chawathe et al., 1994; Arens et al., 1996] or software agents [Etzioni & Weld, 1994; Kirk et al., 1995]) must translate query responses to relational form.

Wrappers are commonly used as such translators. A wrapper is a procedure, specific to a single information resource, that translates a query response to relational form. Wrappers are typically hand-coded; unfortunately, hand-coding is tedious and error-prone.

We seek an automated solution to this problem of constructing wrappers. Natural language processing has been used for similar information-extraction tasks; see [Cowie & Lehner, 1996] for a recent summary. But many information resources do not exhibit the rich grammatical structure such techniques are designed to exploit. Moreover, linguistic approaches tend to be slow, while ideally wrappers should execute quickly, because they are used on-line to satisfy users’ queries.

Wrapper induction is a new technique for automatically constructing wrappers. Our system learns a wrapper by generalizing from example query responses. A PAC model bounds the number of examples needed to generate a satisfactory wrapper. The inductive algorithm requires an oracle to label examples; we solve this labeling problem [Etzioni, 1996] by composing oracles from heuristic knowledge, and we demonstrate that our system degrades gracefully with imperfect heuristics.

We identify HLRT, a class of wrappers which is efficiently learnable, yet expressive enough to handle numerous actual Internet information resources. HLRT is designed for resources that display their content in a tabular layout. HLRT wrappers scan their input for substrings that delimit the information to be extracted. Though our focus is on Internet resources, these learned delimiters need not be HTML tags, but can be arbitrary text.

HLRT corresponds essentially to a class of finite-state automata, so wrapper induction is similar to FSA induction (e.g., [Angluin, 1982]). Since FSAs run in linear time, HLRT satisfies the desire that wrappers be fast. However, since wrappers are used for parsing (rather than just classification), the learned FSA must have a specific state topology. Existing FSA induction algorithms do not make such guarantees, so we have developed a new algorithm targeted specifically at HLRT.

We make the following contributions. First, we formalize the wrapper construction problem as that of inductive generalization. Second, we identify the HLRT wrapper class, which is efficiently learnable yet reasonably expressive. Third, we show how to compose the required oracle from (possibly imperfect) heuristics.

We proceed as follows. In Sec. 2, we describe wrappers. In Sec. 3, we cast wrapper construction as inductive generalization; we then spell out this framework by describing how to learn HLRT (Sec. 4), applying the PAC framework (Sec. 5), and presenting a modular approach to building oracles (Sec. 6). Sec. 7 provides an empirical evaluation of our approach. Finally, Sec. 8 describes related work.

2 Wrappers
A wrapper is a procedure for extracting tuples from a particular information source. Formally, a wrapper is a function from a page\(^1\) to the set of tuples it contains.

\(^1\)We use the term page generically, referring to whatever query response is returned by an information resource.
Figure 2: A partial hierarchy of wrapper biases. Arrows indicate that one bias is more expressive than another.

For example, consider a fictitious information resource that provides a tabular list of countries and their telephone country codes. Suppose that in response to a query, the resource responds as displayed in Fig. 1(a), which was rendered from the HTML shown in (b). Many kinds of wrappers could be written; we consider wrappers that use the positions of particular strings to delimit the extracted text. From (b), it appears that this resource renders tuples by surrounding countries with <i> and </i>, and country codes with <b> and </b>. So one candidate wrapper relies on these four delimiters.

But note that this simple left-right (LR) strategy fails, because not all occurrences of <i>... </i> indicate a country. However, the string <b>... </b> can be used to distinguish the head of the page from the tuples proper. Similarly, <i>... </i> separates the last tuple from the tail. Fig. 1(c) shows ExtractCCs, a wrapper based on this more sophisticated head-left-right-tail (HLRT) approach.

We focus on wrappers that are structurally similar to ExtractCCs. Fig. 1(d) shows the template for HLRT wrappers. Note that instantiating the template with the six strings \( \langle \mathsf{P}, \mathsf{HR}, \mathsf{B}, \mathsf{I}, \mathsf{O}, \mathsf{D} \rangle \) yields ExtractCCs.

Formally, an HLRT wrapper for a domain with \( K \) attributes per tuple is encoded as a vector of \( 2K + 2 \) strings \( \langle h, t, \ell_1, r_1, \ldots, \ell_K, r_K \rangle \). One string \( h \) marks the end of the header, another \( t \) marks the start of the tail, and two strings \( \langle \ell_k \, \mathsf{R}, r_k \rangle \) delimit each of the \( K \) attributes.

We focus on HLRT, but alternatives abound. Fig. 2 illustrates a partial hierarchy of wrapper classes. LR is less expressive than HLRT; for example, the country/code resource can be wrapped by HLRT but not LR. BELR's \( b \) and \( e \) mark the beginning and end of each tuple \( \langle \mathsf{H}, \mathsf{R}, \mathsf{B}, \mathsf{I}, \mathsf{O}, \mathsf{D} \rangle \) yields ExtractCCs.

PAC analysis is used to terminate the learning process, so the system takes as input accuracy \( (e) \) and
confident (δ) parameters.

With this framework in place, we now present the wrapper induction algorithm; see Fig. 3. Wrapper induction proceeds by accumulating a set $\mathcal{E}$ of labeled example pages. On each iteration, BuildHLRT is called with $\mathcal{E}$, which returns wrapper $w$. Learning stops when $w$ satisfies the PAC bound. In Secs. 4–6, we describe the algorithm’s main components:

- **BuildHLRT** constructs an HLRT wrapper from a set of labeled example pages; see Sec. 4.
- $\Pr[E(w) < \varepsilon] > 1 - \delta$ is a PAC-theoretic termination condition, testing whether enough examples have been seen to be confident that a satisfactory wrapper has been learned; see Sec. 5.

**LabelOracle** is a function from a page to a label. In Sec. 6 we describe how to compose a correct labeling oracle from (possibly imperfect) heuristic knowledge.

### 4 Building HLRT wrappers

**BuildHLRT** takes as input a set of labeled pages, and returns an HLRT wrapper that is consistent with each labeled page. A wrapper is consistent with a labeled page if it generates the label for the page. Fig. 4 shows the **BuildHLRT** algorithm.

BuildHLRT reasons about the conditions that must hold if wrapper $\langle h, t, \ell_1, \ell_2, \ldots, \ell_K, r_K \rangle$ is to be consistent. For example, in Fig. 1(b), the string $\langle p \rangle$ is a valid value for $\ell_2$, because $\langle p \rangle$ actually precedes every instance of the second attribute. Such constraints apply to each $r_k$, and to each $\ell_k$ for $k > 1$.

**BuildHLRT** is complicated by the fact that $\ell_1$, $t$, and $h$ interact. For example, to determine whether $\langle p \rangle$ is acceptable as $\ell_1$ (even though the head and tail contain $\langle p \rangle$), BuildHLRT must find an $h$ and $t$ such that $\langle p \rangle$ does in fact reliably mark the start of the first attribute. In this case, $h = \langle p \rangle$ and $t = \langle p \rangle$ are satisfactory. Lines (a–d) in Fig. 4 capture the constraints that $\ell_1$, $t$, and $h$ must satisfy. BuildHLRT examines all possible combinations of $\ell_1$, $h$, and $t$, stopping when it finds values that jointly satisfy these constraints.

To summarize, BuildHLRT iterates over all choices for the $2K + 2$ delimiters, stopping when a consistent wrapper is encountered. BuildHLRT’s search is made more efficient by decomposing the constraint satisfaction problem into three independent subproblems: finding values for (1) the $r_k$; (2) the $\ell_k$ ($k > 1$); and (3) $h$, $t$, and $\ell_1$.

In [Kushmerick, 1997], we prove that: (1) **BuildHLRT** is sound (if BuildHLRT returns a wrapper, then it is consistent) and complete (if a consistent wrapper exists, BuildHLRT finds it); and (2) under reasonable assumptions, BuildHLRT runs in time $O(K N M S^3)$, where each tuple has $K$ attributes, the shortest of the $N$ example pages has length $S$, and $M$ is maximum number of tuples in any single example.

Appendix A formally describes the conditions under which an HLRT wrapper is consistent with a labeled page.

### 5 PAC analysis

PAC analysis answers the question, **How many examples must a learner see to be confident that its hypothesis is good enough—i.e., to be probably approximately correct?**; see [Kearns & Vazirani, 1994] for an introduction. A PAC model defines an error metric over hypothesis: $E(w)$ is the probability that hypothesis $w$ will incorrectly label the next instance. The learning task is then analyzed in order to bound the number of examples which ensure that $\Pr[E(w) > \varepsilon] < \delta$, for any given accuracy parameter $\varepsilon$ and confidence parameter $\delta$. In [Kushmerick, 1997], we prove the following theorem.

**Theorem 1 (HLRT sample complexity)** Suppose BuildHLRT($\mathcal{E}$) returns wrapper $w$, where $\mathcal{E}$ contains collectively $T$ tuples, each with $K$ attributes. If

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\left( 1 - 2 \left( 1 - \frac{\varepsilon}{2} \right)^T \right)^{2K} \left( 1 - 2 \left( 1 - \frac{\varepsilon}{2} \right)^{|\mathcal{E}|} \right)^2 > 1 - \delta,
$$

then $\Pr[E(w) > \varepsilon] < \delta$, for any $0 < \varepsilon < 1$ and $0 < \delta < 1$.

For example, with $\varepsilon = \delta = 0.1$, $K = 4$, and an average of 5 tuples/page, BuildHLRT must examine at least 72 examples to satisfy the PAC criteria.
This bound is relatively tight compared to typical PAC results. For example, the number of possible HLRT wrappers is infinite, but our bound does not depend on the number of wrappers. Thus clearly the stated bound is tighter than obtainable under simple PAC models (e.g., [Valiant, 1984; Blumer et al., 1987]), in which sample complexity grows with the number of hypotheses. The bound is also tighter than obtainable using Vapnik-Chervonenkis analysis [Haussler, 1988]. To understand these results, recall that BuildHLRT is essentially computing common prefixes and suffixes of sets of strings, which are highly constrained after relatively few examples; see [Kushmerick, 1997] for a detailed discussion.

6 Composing oracles

A key to induction is an oracle that labels examples. So far, we have assumed that LabelOracle is provided as input. We now describe how to compose LabelOracle from modular heuristic knowledge, which we call recognizers. A recognizer finds instances of a particular attribute on a page. For example, a country name recognizer would identify the four countries contained in Fig. 1(b)’s HTML. These recognized instances are then corroborated to label the entire page. For example, given a recognizer for countries and another for country codes, corroborate produces an oracle that labels pages containing pairs of these attributes.

Corroboration is trivial if each recognizer is perfect.3 But an important feature of our approach is that it handles imperfect recognizers. Recognizers are either perfect (accept all positive instances and reject all negative instances of their target attribute), incomplete (reject all negative instances but reject some positive instances), unsound (accept all positive instances but accept some negative instances), or unreliable (reject some positive instances and accept some negative instances).

We require that each recognizer be annotated with the kind of error it makes. We expect this annotation to be natural for many kinds of recognizers. For example, a company name recognizer based on Fortune-500 data is incomplete, while a country code recognizer accepting any digit sequence is unsound. The intent is that recognizers are reusable across domains; a company name recognizer, for example, can be used with any information resource displaying companies.

Recall that LabelOracle is a function from a page to a label for the page. A label is an array, where rows correspond to tuples, and columns are attributes. A recognizer is a function from a page to a set of instances (subsequences of the page). The set of recognized instances is a column of the overall label array. The corroboration problem, then, is to build the entire label array from the individual columns. Note that the attributes’ ordering within tuples is not part of the input; the corroboration algorithm must determine this ordering.

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The basic idea of corroboration is that the location of some instances greatly constrains the possible location of others. Suppose recognizer A is unsound and identifies an instance at position 10–20, while perfect recognizer B finds an instance at 14–16. Since attributes never overlap, the A at 10–20 must be a false positive (FP) and thus must be ignored, while the B at 14–16 is a true positive (TP).

In the remainder of this section, we describe corroboration by walking through an example, present the Corrob corroboration algorithm, and describe how our work is extended to handle imperfect recognizers.

Example. Fig. 5 extends the country/code example to include an additional attribute, the country’s capital.4 Corroboration begins by noting the type of error made by each recognizer: in this simple example, assume the recognizer for the codes is perfect, but the country recognizer is incomplete and the capital recognizer is unsound.

Next, note that since the Code recognizer is perfect, all Code instances are TPs. Thus Code can be simply copied to the label array. The incomplete Ctry column is almost as easy: it is copied verbatim, but Code is used to align each Ctry instance. This leaves a “hole” in the Ctry column. Next, the corrobator processes the unsound Cap column. 5–7 must be a FP, because were it a TP, Code would have included an additional instance prior to 5. Next, since 19–25 overlaps with Code’s 18–20, 19–25 must be a FP. Since 22–28 is the only remaining possibility for the first tuple’s Cap instance, 22–28 must be a TP. However, for the second tuple, there is no way to choose between 42–48 and 44–49: one must be a TP and the other a FP, but there is no way to decide. Corroboration thus uses 42–48+44–49, indicating that exactly one of the two instances is a TP. Finally, corroboration rejects 59–65 because it overlaps with 58–60.

The Corrob algorithm. Fig. 6 shows Corrob, an algorithm for corrobating imperfect recognizers, for the case when at least one recognizer is perfect.5 As indicated in the example, Corrob builds the label array by

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3Wrappers are needed even with perfect recognizers, because recognizers might be slow, while wrappers must be fast.

4The indices in this example do not match Fig. 1(b).

5People can be used as perfect recognizers, though we seek to automate wrapper construction as much as possible.
**Corrob** (recognizers \{R_1, \ldots, R_m\}, instances \{I_1^*, \ldots, I_n^*\})

*Notation: \( I_j^* \) is the \( j \)th instance recognized by \( R_k \). \( A \leftarrow \text{BuildArray}\{\{I_j^* : R_k \text{ is perfect or incomplete}\}\) for each \( I_j^* \) such that \( R_k \) is unsound or unrepeatable. If \( I_j^* \) is possibly a TP (based on the TPs in \( A \)), then \( m \leftarrow \text{RowOf}(I_j^*, A) \)

\( A_m, s \leftarrow A_m, s \oplus I_j^* \)

return \( A \)

**BuildArray** (necessarily TP instances \{\( I_1^* \), \ldots, \( I_n^* \)\})

Build array with each \( I_j^* \) installed in the correct cell.

**RowOf**(possibly TP instance \( I_j^* \), array \( A \))

Determine the row \( m \) of \( A \) to which \( I_j^* \) belongs, which is always determined when at least one \( R_k \) is perfect.

**Figure 6: The Corrob algorithm.**

First installing instances recognized by perfect or incomplete recognizers. These TPs are then used to categorize the remaining instances as either necessarily FPs (meaning they can be ignored), or possibly TPs (meaning they are inserted using \( \oplus \)”). In [Kushmerick, 1997], we describe **Corrob** in more detail and prove that it is correct.

**Handling mistakes.** Note that **Corrob**’s output might contain attributes that are missing ("?” indicates attributes falsely rejected by their recognizers) or ambiguous ("@” indicates under-constrained attributes). But **BuildHIRT** assumes that **LabelOracle** produces a perfect label. We now describe how to extend our work to handle this discrepancy.

Missing attributes require only minor changes to **BuildHIRT**: the algorithm must simply generalize from fewer examples. For example, recall the original country generalize from code resource in Fig. 1. Suppose that corroboration yields a label that is correct except that the country Congo is missing. In this case, when learning \( f_1 \), the algorithm generalizes from just the three occurrences of "<\!/\!>\!<\!/>\!<\!>\!<\!>\!<\!>\!<\!>\!"> that precede the recognized instances of the first attribute, and the algorithm may well fail to generate the correct wrapper. Only if the first country name is correctly recognized on a subsequent example page will **BuildHIRT** realize that \( f_1 \) must be a suffix of "<\!/\!>\!<\!/>\!<\!>\!<\!>\!<\!>\!<\!>\!Title>Some Country Codes</F>" as well as of "<\!/\!>\!<\!>\!<\!>\!<\!>\!<\!>\!".

The PAC model must also be extended to accommodate missing attributes. To do so, we generalize Thm. 1 so that, instead of assuming exactly \( N \) head and tail and \( T \) left and right delimiter examples, the model counts the actual numbers, based on the non-missing attributes. So, in the previous example, there are four examples for \( t_2 \) and \( t_1 \), but only three for \( t_1 \) and \( r_1 \), and zero for \( h \).

Ambiguity requires more substantial changes. There are two kinds of ambiguity. First, as described earlier, **Corrob** uses "@" to indicate that more than one recognized instance is consistent with a particular cell in the label array. Second, recall that **Corrob** must determine the ordering of attributes within tuples. But the recognized instances may be consistent with more than one ordering. For example, in Fig. 5, a valid label exists for the ordering \( \text{Cap, Ctry, Code} \) as well as for \( \text{Ctry, Code, Cap} \). (We previously ignored ordering ambiguity to simplify the presentation of **Corrob**.)

We extend **BuildHIRT** to handle both types of ambiguity as follows. An ambiguous label actually corresponds to a set of unambiguous labels, one for each way to resolve each ambiguity. Exactly one such label is correct; the rest either contain FPs or correspond to an incorrect attribute ordering. Faced with ambiguity, **BuildHIRT** iterates over each possibility, stopping when a wrapper can be induced.

Clearly the number of such possibilities grows exponentially in the number of ambiguities. In practice this growth is tolerable for both unsound and incomplete recognizers, even with very high error rates; see Sec. 7. However, **Corrob** is impractical for unreliable recognizers, because the number of ambiguities grows quickly with an unreliable recognizer’s error rate.

We extend the PAC model to handle ambiguous labels by accounting for situations in which **BuildHIRT** considers an incorrect way to resolve a label’s ambiguity, and yet a consistent wrapper exists anyway. For example, in Fig. 5(d), if the second tuple’s Cap attribute is actually 42–48 rather than 44–49, but **BuildHIRT** tries 44–49 first and successfully finds a wrapper, then **BuildHIRT** has probably made a mistake. Similarly, if **BuildHIRT** considers the ordering \( \{\text{Cap, Ctry, Code}\} \) before \( \{\text{Ctry, Code, Cap}\} \), then **BuildHIRT** is probably wrong if it finds a consistent wrapper.

We model this effect by assuming that such a situation happens with probability at most \( \mu \) per opportunity, and thus the left-hand side of the bound in Thm. 1 is multiplied by \((1 - \mu)^R\), where \( R \) is the number of opportunities that a mistake of this type could have occurred as **BuildHIRT** was enumerating the possible labels. In practice, we find that \( \mu \) is extremely close to zero and \( R \) is relatively small, and thus ambiguity has a negligible effect on the PAC results. In [Kushmerick, 1997], we compare this noise model to others in the PAC literature.

## 7 Empirical evaluation

In this section, we present preliminary evidence demonstrating the feasibility of **HIRT** learning. Our LISP implementation requires between 4 and 40 SGI Indy CPU seconds per example page, depending on the domain. Normalizing for the number of attributes (\( K \)) and the size of the example pages, our system requires about 0.21 CPU sec. per attribute per KB of example data.

Our first experiment verifies the utility of the **HIRT** bias. Learnability aside, can a significant fraction of interesting information resources be wrapped by **HIRT**? We surveyed 100 Internet resources selected randomly from an independent organization’s index (search.com), and found that 48% can be wrapped by **HIRT**. We take this result to be evidence that **HIRT** is genuinely useful.

Our second experiment measures the robustness of the
system to the recognizers' error rates. We tested our system on (i) the OKRA email service, okra.ucr.edu/okra; and (ii) the BIGBOOK telephone directory, bigbook.com.

By hand, we constructed perfect recognizers for each attribute; OKRA has four attributes and BIGBOOK has six. As a baseline, we ran our system with these perfect recognizers. We then increased the error rates up to 40% (creating both incomplete and unsound recognizers for each attribute) and increased the number of imperfect recognizers from zero until all but one were imperfect. We tested our system using two termination conditions: (a) we ran the system until the PAC criteria was satisfied (for \( \epsilon = \delta = 0.1 \)); and (b) we required that the learned wrapper be 100% correct on a suite of test pages.

Fig. 7 shows the number of pages needed to induce a wrapper, as a function of the error rate, for each termination condition, and for each domain. Each curve within a graph represents a different number of imperfect recognizers. For example, the points marked “perfect” represent trials in which all recognizers are perfect, while the points marked “30% error rate of each recognizer” on the “2 imperfect recognizers” curves indicate trials in which two of the recognizers are imperfect (yielding either 30% FPs or 30% FNs) while the remaining recognizers are perfect. Thus in each graph, increasing the abscissa or examining curves with additional imperfect recognizers corresponds to trials in which the recognizers make more mistakes.

Figs. 7(i–ii,b) indicate that, from a practical perspective, relatively few examples are needed before the system learns the correct wrapper; across all conditions, about 4.9 examples suffice for OKRA and 29 for BIGBOOK. We conclude that the number of examples required is small enough that HLRT wrapper induction is practical, even for extremely high recognizer error rates.

Figs. 7(i–ii,a) show that the PAC bound is relatively loose. Across all conditions, about 106 examples are needed required to satisfy the PAC criteria. Thus the PAC bound is too loose by about an order of magnitude. We conclude that the current PAC model is too weak to tightly constrain the induction process. Nevertheless, since wrapper construction is intended to be an off-line process, the bound is not so loose as to be useless.

Finally, we have developed WIEN (pronounced “Vienna”), a wrapper induction environment. Using a Web browser, a user shows WIEN an example information resource page, and then uses the mouse to label the page. WIEN then tries to learn a wrapper for the resource. When the user shows WIEN a second example, it uses the learned wrapper to automatically label the new example. The user then corrects any mistakes, and WIEN generalizes from both examples. This process repeats until the user is satisfied. WIEN provides a complete implementation of BuildHLRT, though the user is assumed to label pages perfectly, so WIEN implements neither attribute recognition nor corroboration.

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7Recall that Corrob is impractical for unreliable recognizers and requires at least one perfect recognizer.

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Figure 7: Effect on learning curve of recognizer error, in the (i) OKRA and (ii) BIGBOOK domains, for the (a) PAC and (b) 100% accurate termination conditions.

8 Related work

As suggested at the outset, wrapper construction is motivated by the software engineering issues involved with deploying software systems that rely on external information resources; examples include [Chawathe et al., 1994; Etzioni & Weld, 1994; Arens et al., 1996; Kirk et al., 1995]. While data interchange protocols (e.g. KQML [Finin et al., 1994]) have been proposed to address these issues, they require cooperation on the part of information providers, and such cooperation is rare.

From a formal perspective, in Sec. 1 we discussed the relationship between HLRT and FSA induction.

From an application perspective, our work is similar to [Ashish & Knoblock, 1997]. Their system learns a more expressive wrapper class than HLRT, but relies on many
heuristics that are specific to HTML. In contrast, our system treats HTML tags just as ordinary text. Moreover, their system requires human intervention to correct its mistakes, while our co-segmentation process is intended to correct word-mistakes automatically. A second related application is SHOPBOT [Doorenbos et al., 1997]. Though in many respects SHOPBOT is more ambitious, its wrapper language is less expressive than HLRT.

Finally, our recognition knowledge is similar to work on semantically labeling natural text, such as the MUC-6 “Named Entity” task [DARPA, 1995], though relatively little work has been done on co-segmenting multiple such knowledge sources.

9 Conclusions

Wrapper induction is a new technique for automatically constructing wrappers. We have made three contributions. First, we have formalized the wrapper construction problem as prediction. Second, we have defined the HLRT bias, which is efficiently learnable in this framework. Third, we have shown how to use heuristic knowledge to compose the algorithm’s oracle. Though our work has involved primarily Internet information resources, we expect that our results are applicable to similar information-extraction tasks in other domains.

We intend to extend our framework in several ways. In addition to the biases shown in Fig. 2, we want to design wrappers that can handle non-tabular pages, such as pages organized hierarchically. The research issues involve exploring the tradeoff between expressiveness and learnability. We also hope to tighten the PAC model so it is more useful in practice as well as more predictive of observed learning curves.

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A HLRT consistency conditions

In this Appendix, we list the conditions under which HLRT wrapper \( w = \{ h, t, \ell_1, \ldots, \ell_K \} \) outputs label \( L = \{ \{ b_1, e_1 \}, \ldots, \{ b_K, e_K \} \} \) for page \( P \). This notation indicates that that \( P \) contains \( M \) tuples having \( K \) attributes each, where the \( b \) attribute of the \( m \) tuple begins at index \( b_{m,k} \) of \( P \) and ends at \( e_{m,k} \). Note that \( L \) partitions \( P \) as follows:\footnote{\( \ell_i \) indicates concatenation: \( P = S_0, A_1, \ldots, A_{l_i-1}, S_{l_i} \) \( A_{l_i} \cdots S_{l_i-1}, A_{l_{i+1}}, \cdots, A_{l_{M-1}}, S_{l_M} \). The \( A_i \)s are the attribute values: \( A_i = P[b_{m,k}, e_{m,k}] \). The \( S_m \)s separate the tuples, and attributes within a tuple: \( S_m, P[b_{m,k}, e_{m,k}] \) \( S_m \) (except that \( S_0 = P[0, b_1] \), \( S_M = P[e_{m,k}, P] \), and \( S_0 \) and \( S_M \) are consistent with \( P \) and \( L \) iff:}

1. the \( \ell_i \) immediately preceeds their attributes
2. the \( \ell_i \) follow (but don’t occur within) their attributes
3. \( h \) occurs in the head and \( t \) occurs in the tail
4. \( t \) never precedes \( \ell_i \) in an inter-tuple separator
5. \( \ell_i \) doesn’t occur between \( h \) and \( t \) in the head (\( S_0, h \) \( t \) \( \ell_i \) \( S_M \))
6. \( \ell_i \) in the tail

\[ \forall \begin{cases} \alpha_{m,k} / h \neq \emptyset \land \forall m, k > 1 \{ S_m, h \} / \ell_i = 0 \end{cases} \]
\[ \forall \begin{cases} \ell_i \neq \emptyset \land \forall m, k \neq i \{ S_m, h \} / \ell_i = S_m, k \end{cases} \]
\[ \forall \begin{cases} h \leq \ell_i \leq t \end{cases} \]
\[ \forall \begin{cases} t \neq \ell_i \end{cases} \]
\[ \forall \begin{cases} S_0, h \neq \emptyset \land \forall m, k \neq i \{ S_m, h \} / \ell_i = \emptyset \end{cases} \]
\[ \forall \begin{cases} S_M, t \neq \emptyset \land \forall m, k \neq i \{ S_m, h \} / \ell_i = \emptyset \end{cases} \]
\[ \forall \begin{cases} S_0, h \leq \ell_i \leq t \end{cases} \]
\[ \forall \begin{cases} t \neq \ell_i \end{cases} \]

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